

Arbeidshefte

Rektangelsum

La f være en funksjon i intervallet $[a, b]$, og $P = (x_0, x_1, \dots, x_n)$ være en oppdeling av intervallet som er slik at

$$a = x_0 < x_1 < x_2 < \dots < x_{n-1} < x_n = b$$

En Riemannsum S av f over $[a, b]$ med partisjonen P er da definert som

$$S = \sum_{i=1}^n f(x_i) \Delta x_i$$

der

$$\Delta x_i = x_i - x_{i-1}$$

$\Delta x = \frac{b-a}{n}$, da blir x -verdiene : $\{a, a + \Delta x, a + 2\Delta x, a + 3\Delta x, \dots, a + (n-1)\Delta x, a + n\Delta x = b, \}$

Riemannsum - venstre

$$S_v = \Delta x (f(a) + f(a + \Delta x) + f(a + 2\Delta x) + \dots + f(b - \Delta x))$$

Riemannsum - høyre

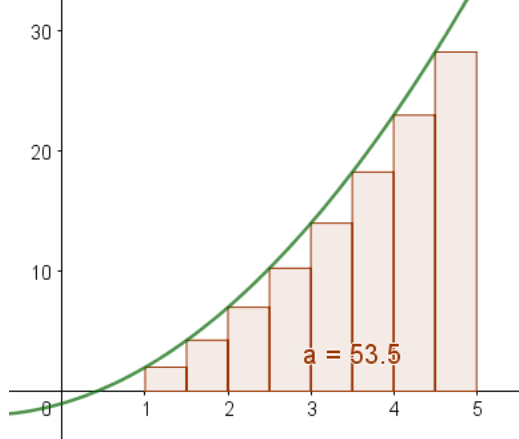
$$S_h = \Delta x (f(a + \Delta x) + f(a + 2\Delta x) + \dots + f(b - \Delta x), f(b))$$

Riemannsum - midtpunkt

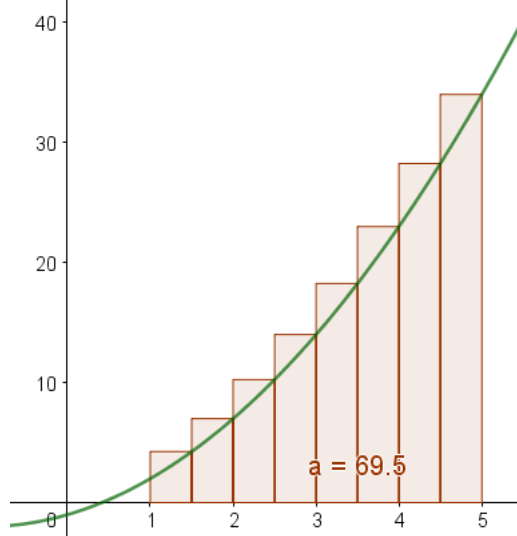
$$S_m = \Delta x (f(a + \frac{\Delta x}{2}) + f(a + \frac{3\Delta x}{2}) + \dots + f(b - \frac{\Delta x}{2}))$$

$$f(x) = x^2 + 2x - 1$$

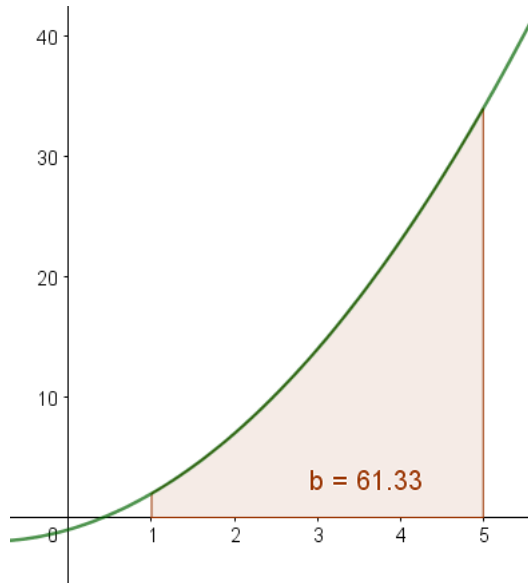
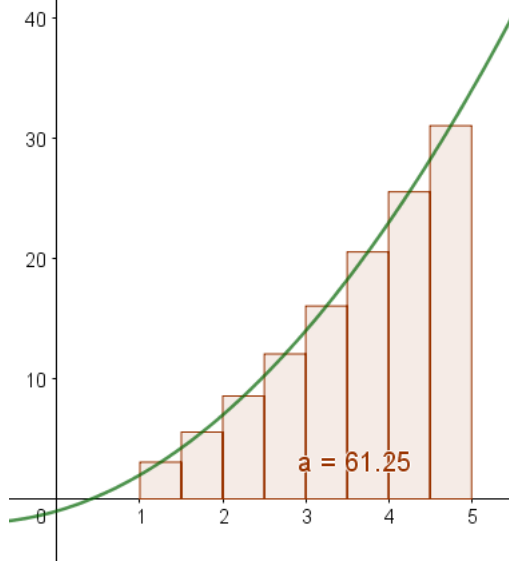
CAS : Rektangelsum(f,1,5,8,0)



CAS : Rektangelsum(f,1,5,8,1)



CAS : Rektangelsum(f,1,5,8,0.5)



Program

```
1 import numpy as np
2 def f(x):
3     return x**2+2*x-1
4
5 xStart = 1
6 xStop = 5
7 dx = 0.5
8 n = int((xStop-xStart)/dx)
9 xVerdier = np.linspace(xStart, xStop, n+1)
10
11 sum = 0
12 print(xVerdier[: -1])
13
14 for i in xVerdier[: -1]:
15     sum += f(i)*dx
16 print(sum)
17
18 sum = 0
19 print(xVerdier[1:])
20
21 for i in xVerdier[1:]:
22     sum += f(i)*dx
23 print(sum)
24
25 sum = 0
26 print(xVerdier[: -1]+dx/2)
27
28 for i in xVerdier[: -1]:
29     sum += f(i+dx/2)*dx
30 print(sum)
```

Output

```
[ 1.  1.5  2.  2.5  3.  3.5  4.  4.5 ]
53.5
[ 1.5  2.  2.5  3.  3.5  4.  4.5  5. ]
69.5
[ 1.25  1.75  2.25  2.75  3.25  3.75  4.25  4.75 ]
61.25
>>>
```